

The University of the State of New York
REGENTS HIGH SCHOOL EXAMINATION

GEOMETRY

Friday, June 20, 2014 — 1:15 to 4:15 p.m., only

Student Name: _____

School Name: _____

The possession or use of any communications device is strictly prohibited when taking this examination. If you have or use any communications device, no matter how briefly, your examination will be invalidated and no score will be calculated for you.

Print your name and the name of your school on the lines above.

A separate answer sheet for Part I has been provided to you. Follow the instructions from the proctor for completing the student information on your answer sheet.

This examination has four parts, with a total of 38 questions. You must answer all questions in this examination. Record your answers to the Part I multiple-choice questions on the separate answer sheet. Write your answers to the questions in Parts II, III, and IV directly in this booklet. All work should be written in pen, except for graphs and drawings, which should be done in pencil. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc.

The formulas that you may need to answer some questions in this examination are found at the end of the examination. This sheet is perforated so you may remove it from this booklet.

Scrap paper is not permitted for any part of this examination, but you may use the blank spaces in this booklet as scrap paper. A perforated sheet of scrap graph paper is provided at the end of this booklet for any question for which graphing may be helpful but is not required. You may remove this sheet from this booklet. Any work done on this sheet of scrap graph paper will *not* be scored.

When you have completed the examination, you must sign the statement printed at the end of the answer sheet, indicating that you had no unlawful knowledge of the questions or answers prior to the examination and that you have neither given nor received assistance in answering any of the questions during the examination. Your answer sheet cannot be accepted if you fail to sign this declaration.

Notice...

A graphing calculator, a straightedge (ruler), and a compass must be available for you to use while taking this examination.

DO NOT OPEN THIS EXAMINATION BOOKLET UNTIL THE SIGNAL IS GIVEN.

Part I

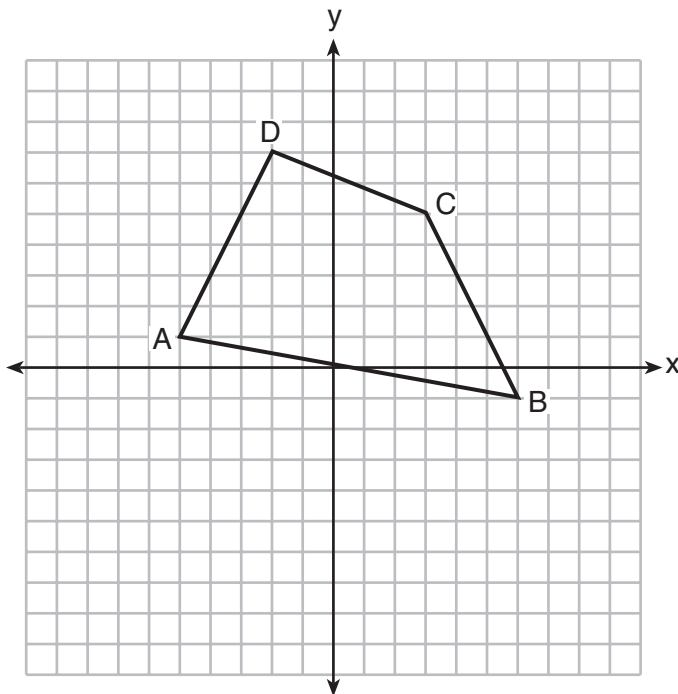
Answer all 28 questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. For each statement or question, choose the word or expression that, of those given, best completes the statement or answers the question. Record your answers on your separate answer sheet. [56]

Use this space for
computations.

1 Plane \mathcal{P} is parallel to plane \mathcal{Q} . If plane \mathcal{P} is perpendicular to line ℓ , then plane \mathcal{Q}

- (1) contains line ℓ
- (2) is parallel to line ℓ
- (3) is perpendicular to line ℓ
- (4) intersects, but is not perpendicular to line ℓ

2 In the diagram below, quadrilateral $ABCD$ has vertices $A(-5,1)$, $B(6,-1)$, $C(3,5)$, and $D(-2,7)$.

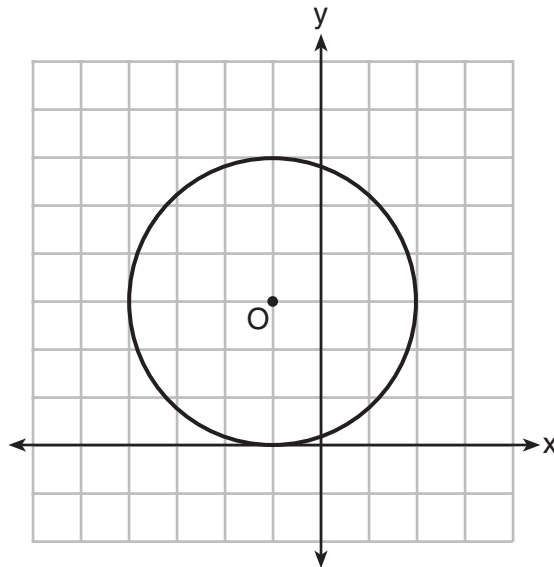


What are the coordinates of the midpoint of diagonal \overline{AC} ?

- (1) $(-1,3)$
- (2) $(1,3)$
- (3) $(1,4)$
- (4) $(2,3)$

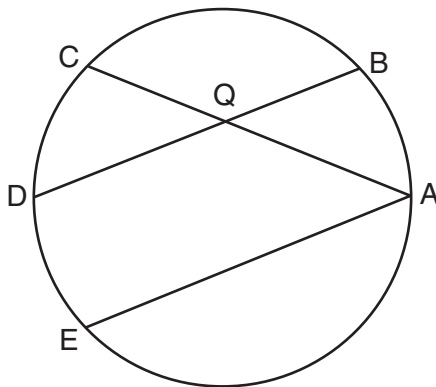
Use this space for computations.

8 Circle O is graphed on the set of axes below. Which equation represents circle O ?



- (1) $(x + 1)^2 + (y - 3)^2 = 9$
- (2) $(x - 1)^2 + (y + 3)^2 = 9$
- (3) $(x + 1)^2 + (y - 3)^2 = 6$
- (4) $(x - 1)^2 + (y + 3)^2 = 6$

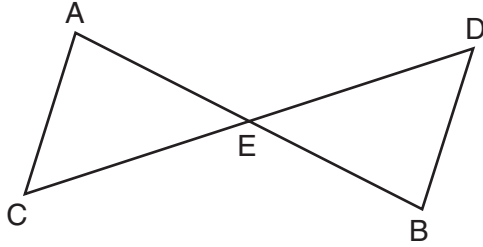
9 In the diagram of the circle shown below, chords \overline{AC} and \overline{BD} intersect at Q , and chords \overline{AE} and \overline{BD} are parallel.



Which statement must always be true?

- (1) $\widehat{AB} \cong \widehat{CD}$
- (2) $\widehat{DE} \cong \widehat{CD}$
- (3) $\widehat{AB} \cong \widehat{DE}$
- (4) $\widehat{BD} \cong \widehat{AE}$

10 In the diagram below, $\triangle AEC \cong \triangle BED$.



Which statement is *not* always true?

- (1) $\overline{AC} \cong \overline{BD}$ (3) $\angle EAC \cong \angle EBD$
(2) $\overline{CE} \cong \overline{DE}$ (4) $\angle ACE \cong \angle DBE$

11 What is the length of \overline{RS} with $R(-2,3)$ and $S(4,5)$?

- (1) $2\sqrt{2}$ (3) $2\sqrt{10}$
(2) 40 (4) $2\sqrt{17}$

12 What are the truth values of the statement “Two is prime” and its negation?

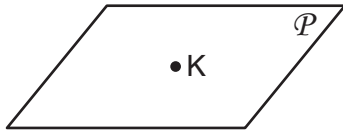
- (1) The statement is false and its negation is true.
(2) The statement is false and its negation is false.
(3) The statement is true and its negation is true.
(4) The statement is true and its negation is false.

13 A regular polygon has an exterior angle that measures 45° . How many sides does the polygon have?

- (1) 10 (3) 6
(2) 8 (4) 4

Use this space for
computations.

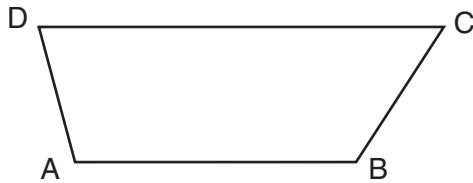
18 In the diagram below, point K is in plane \mathcal{P} .



How many lines can be drawn through K , perpendicular to plane \mathcal{P} ?

- (1) 1 (3) 0
(2) 2 (4) an infinite number

19 In the diagram below, \overline{AB} and \overline{CD} are bases of trapezoid $ABCD$.



(Not drawn to scale)

If $m\angle B = 123$ and $m\angle D = 75$, what is $m\angle C$?

- (1) 57 (3) 105
(2) 75 (4) 123

20 What is the equation of a line passing through the point $(4, -1)$ and parallel to the line whose equation is $2y - x = 8$?

- (1) $y = \frac{1}{2}x - 3$ (3) $y = -2x + 7$
(2) $y = \frac{1}{2}x - 1$ (4) $y = -2x + 2$

**Use this space for
computations.**

21 The image of rhombus $VWXY$ preserves which properties under the transformation $T_{2,-3}$?

- (1) parallelism, only (3) both parallelism and orientation
(2) orientation, only (4) neither parallelism nor orientation

22 The equation of a circle is $(x - 3)^2 + y^2 = 8$. The coordinates of its center and the length of its radius are

- (1) $(-3,0)$ and 4 (3) $(-3,0)$ and $2\sqrt{2}$
(2) $(3,0)$ and 4 (4) $(3,0)$ and $2\sqrt{2}$

23 Which statement has the same truth value as the statement “If a quadrilateral is a square, then it is a rectangle”?

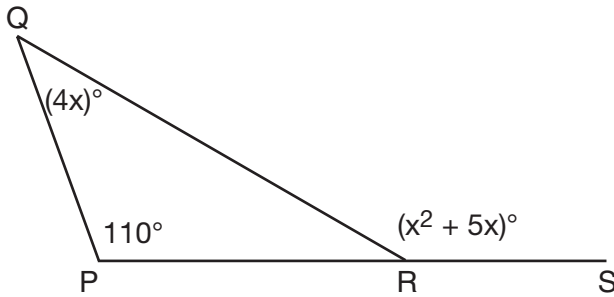
- (1) If a quadrilateral is a rectangle, then it is a square.
(2) If a quadrilateral is a rectangle, then it is not a square.
(3) If a quadrilateral is not a square, then it is not a rectangle.
(4) If a quadrilateral is not a rectangle, then it is not a square.

24 The three medians of a triangle intersect at a point. Which measurements could represent the segments of one of the medians?

- (1) 2 and 3 (3) 3 and 6
(2) 3 and 4.5 (4) 3 and 9

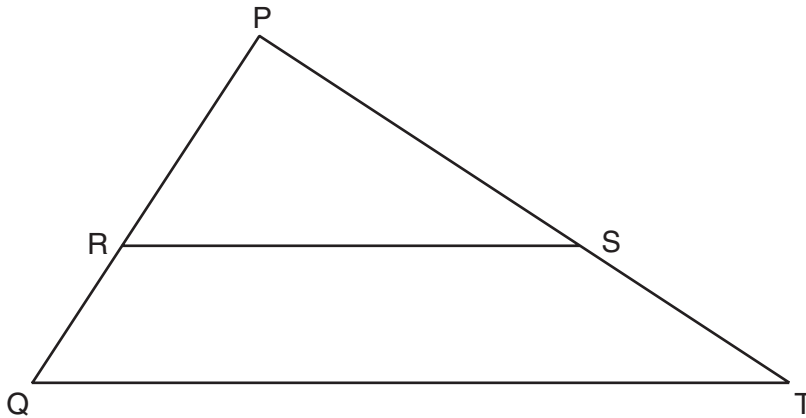
Use this space for computations.

- 25 In the diagram of $\triangle PQR$ shown below, \overline{PR} is extended to S , $m\angle P = 110$, $m\angle Q = 4x$, and $m\angle QRS = x^2 + 5x$.



What is $m\angle Q$?

- (1) 44
(2) 40
(3) 11
(4) 10
- 26 Triangle PQT with $\overline{RS} \parallel \overline{QT}$ is shown below.



If $PR = 12$, $RQ = 8$, and $PS = 21$, what is the length of \overline{PT} ?

- (1) 14
(2) 17
(3) 35
(4) 38

Use this space for
computations.

27 In the diagram of \overline{WXYZ} below, $\overline{WY} \cong \overline{XZ}$.



Which reasons can be used to prove $\overline{WX} \cong \overline{YZ}$?

- (1) reflexive property and addition postulate
- (2) reflexive property and subtraction postulate
- (3) transitive property and addition postulate
- (4) transitive property and subtraction postulate

28 The coordinates of the endpoints of the diameter of a circle are $(2,0)$ and $(2,-8)$. What is the equation of the circle?

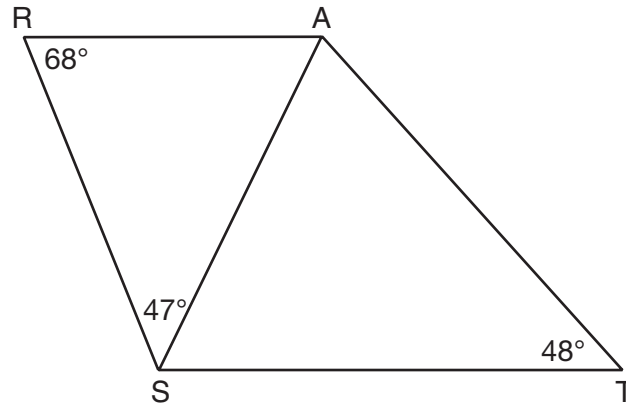
- (1) $(x - 2)^2 + (y + 4)^2 = 16$
 - (2) $(x + 2)^2 + (y - 4)^2 = 16$
 - (3) $(x - 2)^2 + (y + 4)^2 = 8$
 - (4) $(x + 2)^2 + (y - 4)^2 = 8$
-

Part II

Answer all 6 questions in this part. Each correct answer will receive 2 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [12]

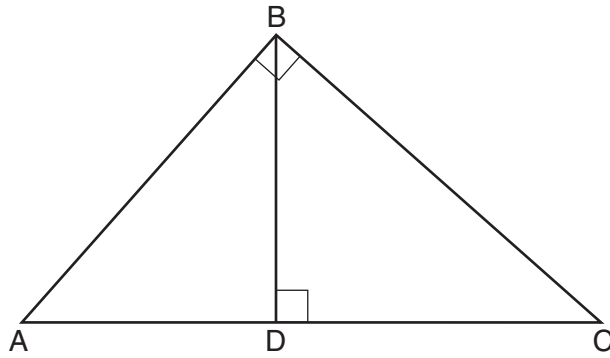
29 The coordinates of the endpoints of \overline{BC} are $B(5,1)$ and $C(-3,-2)$. Under the transformation R_{90} , the image of \overline{BC} is $\overline{B'C'}$. State the coordinates of points B' and C' .

30 As shown in the diagram below, \overline{AS} is a diagonal of trapezoid $STAR$, $\overline{RA} \parallel \overline{ST}$, $m\angle ATS = 48$, $m\angle RSA = 47$, and $m\angle ARS = 68$.



Determine and state the longest side of $\triangle SAT$.

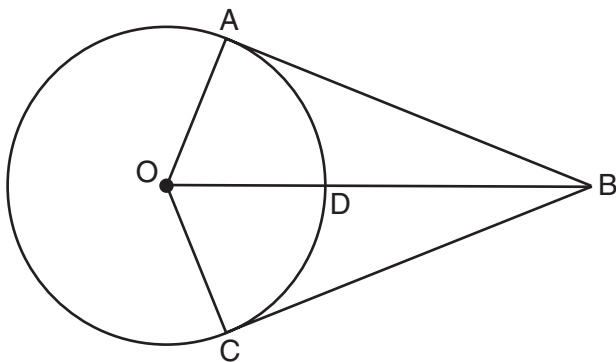
31 In right triangle ABC shown below, altitude \overline{BD} is drawn to hypotenuse \overline{AC} .



If $AD = 8$ and $DC = 10$, determine and state the length of \overline{AB} .

32 Two prisms with equal altitudes have equal volumes. The base of one prism is a square with a side length of 5 inches. The base of the second prism is a rectangle with a side length of 10 inches. Determine and state, in inches, the measure of the width of the rectangle.

33 As shown in the diagram below, \overline{BO} and tangents \overline{BA} and \overline{BC} are drawn from external point B to circle O . Radii \overline{OA} and \overline{OC} are drawn.



If $OA = 7$ and $DB = 18$, determine and state the length of \overline{AB} .

34 Triangle RST is similar to $\triangle XYZ$ with $RS = 3$ inches and $XY = 2$ inches. If the area of $\triangle RST$ is 27 square inches, determine and state the area of $\triangle XYZ$, in square inches.

Part III

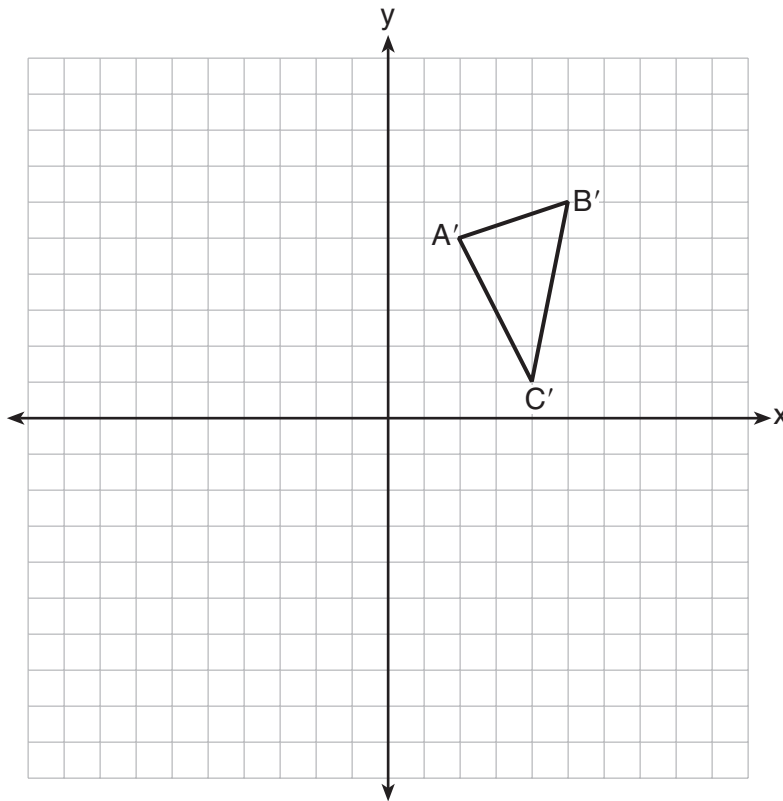
Answer all 3 questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [12]

35 The graph below shows $\triangle A'B'C'$, the image of $\triangle ABC$ after it was reflected over the y -axis.

Graph and label $\triangle ABC$, the pre-image of $\triangle A'B'C'$.

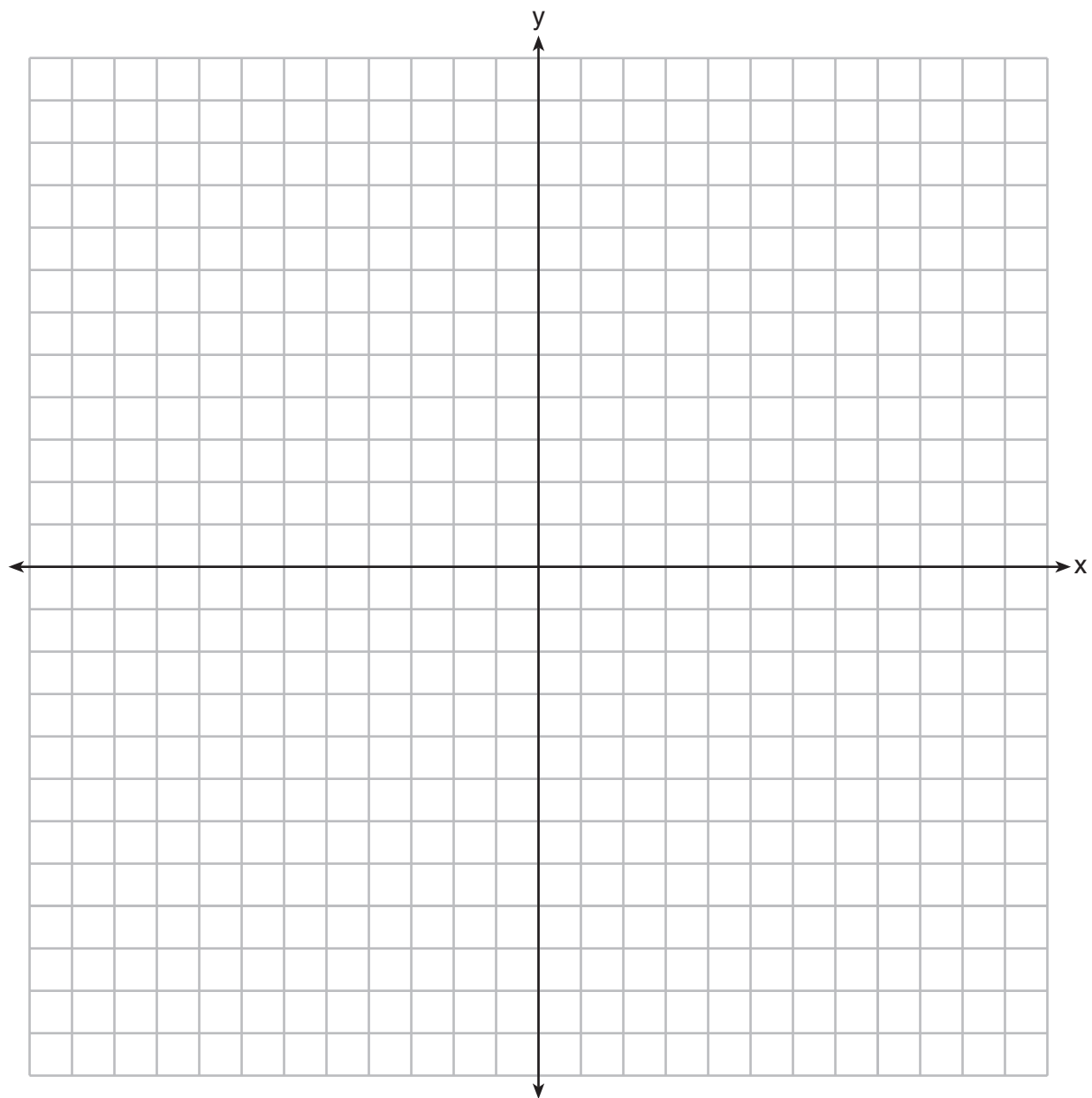
Graph and label $\triangle A''B''C''$, the image of $\triangle A'B'C'$ after it is reflected through the origin.

State a single transformation that will map $\triangle ABC$ onto $\triangle A''B''C''$.



36 On the set of axes below, sketch the locus of points 2 units from the x -axis and sketch the locus of points 6 units from the point $(0,4)$.

Label with an **X** all points that satisfy both conditions.



37 Using a compass and straightedge, construct an equilateral triangle with \overline{AB} as a side.

Using this triangle, construct a 30° angle with its vertex at A.
[Leave all construction marks.]



Part IV

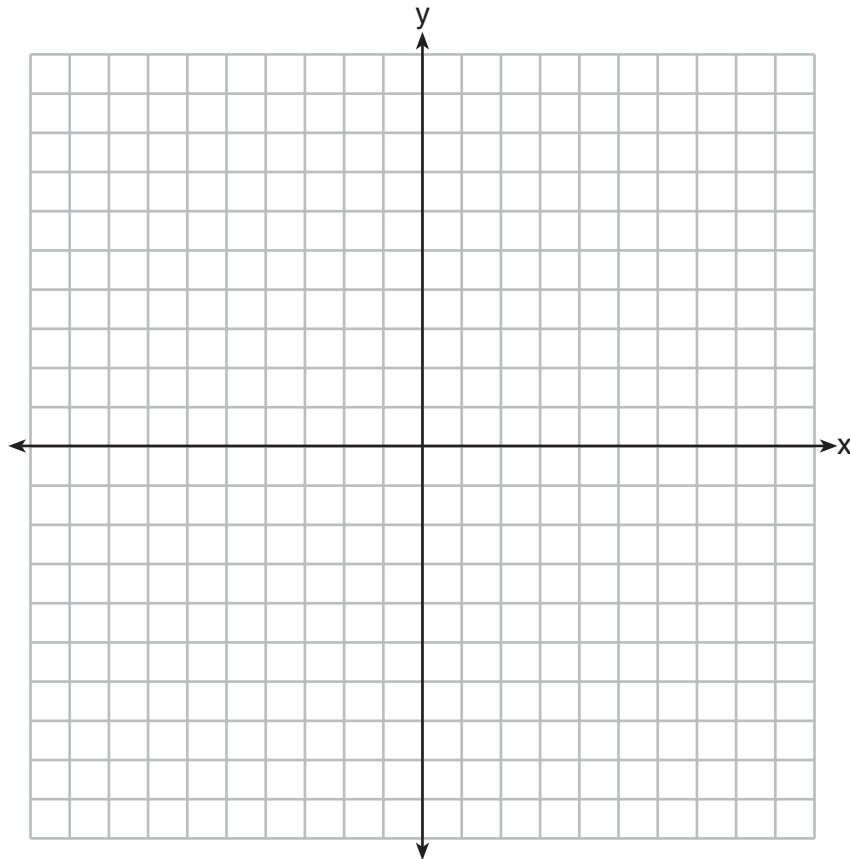
Answer the question in this part. A correct answer will receive 6 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. A correct numerical answer with no work shown will receive only 1 credit. The answer should be written in pen, except for graphs and drawings, which should be done in pencil. [6]

38 The vertices of quadrilateral $JKLM$ have coordinates $J(-3,1)$, $K(1,-5)$, $L(7,-2)$, and $M(3,4)$.

Prove that $JKLM$ is a parallelogram.

Prove that $JKLM$ is *not* a rhombus.

[The use of the set of axes below is optional.]



Reference Sheet

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Volume	Cylinder	$V = Bh$ where B is the area of the base
	Pyramid	$V = \frac{1}{3}Bh$ where B is the area of the base
	Right Circular Cone	$V = \frac{1}{3}Bh$ where B is the area of the base
	Sphere	$V = \frac{4}{3}\pi r^3$

Lateral Area (L)	Right Circular Cylinder	$L = 2\pi rh$
	Right Circular Cone	$L = \pi rl$ where l is the slant height

Surface Area	Sphere	$SA = 4\pi r^2$
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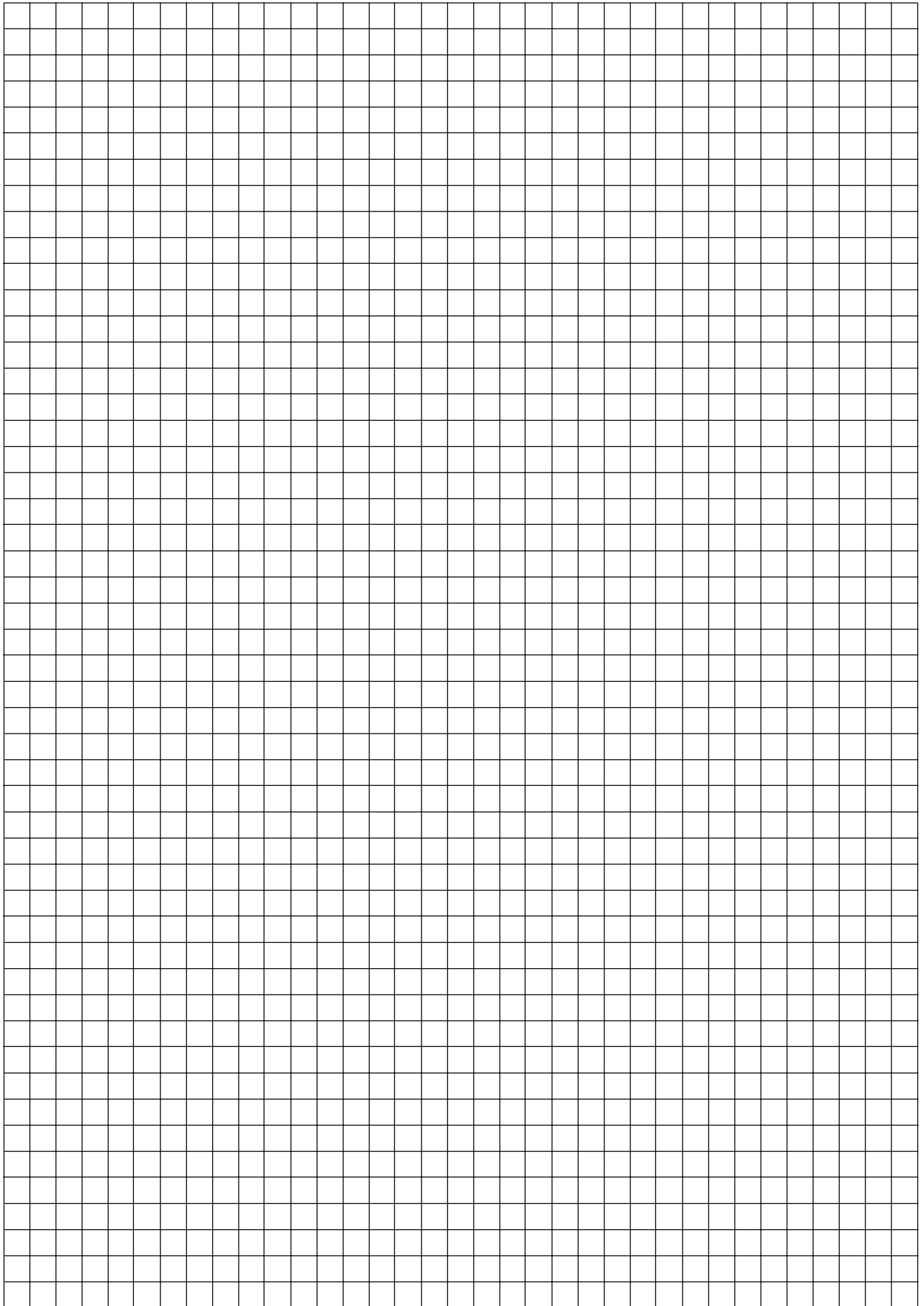
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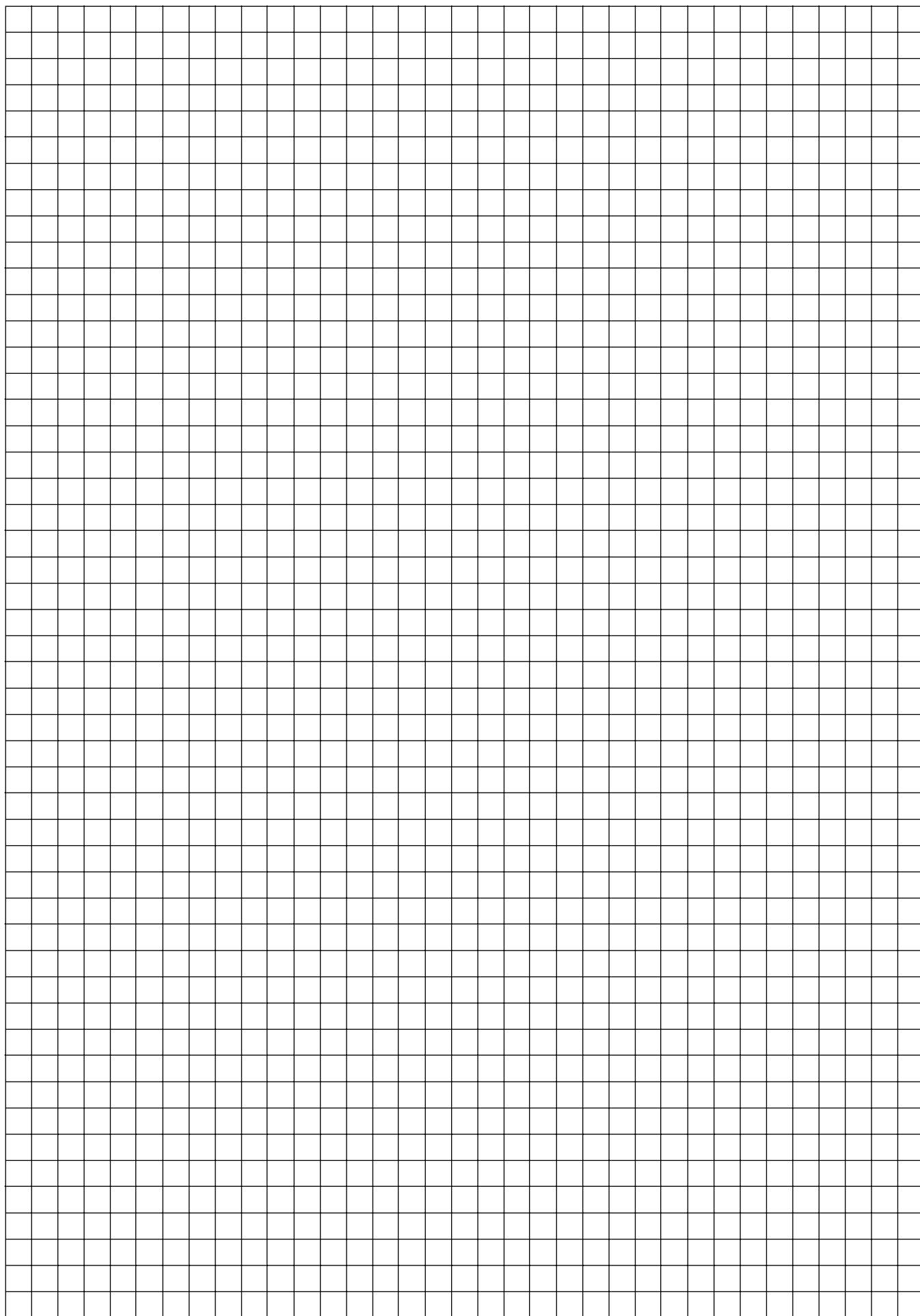
Scrap Graph Paper — This sheet will *not* be scored.

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