

# FOR TEACHERS ONLY

The University of the State of New York

## REGENTS HIGH SCHOOL EXAMINATION

### INTEGRATED ALGEBRA

Thursday, August 13, 2009 — 8:30 to 11:30 a.m., only

### SCORING KEY AND RATING GUIDE

#### **Mechanics of Rating**

The following procedures are to be followed for scoring student answer papers for the Regents Examination in Integrated Algebra. More detailed information about scoring is provided in the publication *Information Booklet for Scoring the Regents Examination in Integrated Algebra*.

Use only *red* ink or *red* pencil in rating Regents papers. Do *not* attempt to correct the student's work by making insertions or changes of any kind. Use check marks to indicate student errors.

Unless otherwise specified, mathematically correct variations in the answers will be allowed. Units need not be given when the wording of the questions allows such omissions.

Each student's answer paper is to be scored by a minimum of three mathematics teachers. On the back of the student's detachable answer sheet, raters must enter their initials in the boxes next to the questions they have scored and also write their name in the box under the heading "Rater's/Scorer's Name."

Raters should record the student's scores for all questions and the total raw score on the student's detachable answer sheet. Then the student's total raw score should be converted to a scaled score by using the conversion chart that will be posted on the Department's web site <http://www.emsc.nysesd.gov/osa/> on Thursday, August 13, 2009. The student's scaled score should be entered in the box provided on the student's detachable answer sheet. The scaled score is the student's final examination score.

INTEGRATED ALGEBRA – *continued***Part I**

Allow a total of 60 credits, 2 credits for each of the following. Allow credit if the student has written the correct answer instead of the numeral 1, 2, 3, or 4.

(1) 2	(9) 2	(17) 2	(25) 3
(2) 1	(10) 4	(18) 1	(26) 2
(3) 4	(11) 1	(19) 3	(27) 4
(4) 1	(12) 4	(20) 1	(28) 4
(5) 3	(13) 4	(21) 3	(29) 3
(6) 1	(14) 2	(22) 2	(30) 2
(7) 3	(15) 1	(23) 3	
(8) 3	(16) 2	(24) 1	

Updated information regarding the rating of this examination may be posted on the New York State Education Department's web site during the rating period. Check this web site <http://www.emsc.nysesd.gov/osa/> and select the link "Examination Scoring Information" for any recently posted information regarding this examination. This site should be checked before the rating process for this examination begins and several times throughout the Regents examination period.

### **General Rules for Applying Mathematics Rubrics**

#### **I. General Principles for Rating**

The rubrics for the constructed-response questions on the Regents Examination in Integrated Algebra are designed to provide a systematic, consistent method for awarding credit. The rubrics are not to be considered all-inclusive; it is impossible to anticipate all the different methods that students might use to solve a given problem. Each response must be rated carefully using the teacher's professional judgment and knowledge of mathematics; all calculations must be checked. The specific rubrics for each question must be applied consistently to all responses. In cases that are not specifically addressed in the rubrics, raters must follow the general rating guidelines in the publication *Information Booklet for Scoring the Regents Examination in Integrated Algebra*, use their own professional judgment, confer with other mathematics teachers, and/or contact the consultants at the State Education Department for guidance. During each Regents examination administration period, rating questions may be referred directly to the Education Department. The contact numbers are sent to all schools before each administration period.

#### **II. Full-Credit Responses**

A full-credit response provides a complete and correct answer to all parts of the question. Sufficient work is shown to enable the rater to determine how the student arrived at the correct answer.

When the rubric for the full-credit response includes one or more examples of an acceptable method for solving the question (usually introduced by the phrase "such as"), it does not mean that there are no additional acceptable methods of arriving at the correct answer. Unless otherwise specified, mathematically correct alternative solutions should be awarded credit. The only exceptions are those questions that specify the type of solution that must be used; e.g., an algebraic solution or a graphic solution. A correct solution using a method other than the one specified is awarded half the credit of a correct solution using the specified method.

#### **III. Appropriate Work**

*Full-Credit Responses:* The directions in the examination booklet for all the constructed-response questions state: "Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, charts, etc." The student has the responsibility of providing the correct answer **and** showing how that answer was obtained. The student must "construct" the response; the teacher should not have to search through a group of seemingly random calculations scribbled on the student paper to ascertain what method the student may have used.

*Responses With Errors:* Rubrics that state "Appropriate work is shown, but ..." are intended to be used with solutions that show an essentially complete response to the question but contain certain types of errors, whether computational, rounding, graphing, or conceptual. If the response is incomplete; i.e., an equation is written but not solved or an equation is solved but not all of the parts of the question are answered, appropriate work has **not** been shown. Other rubrics address incomplete responses.

#### **IV. Multiple Errors**

*Computational Errors, Graphing Errors, and Rounding Errors:* Each of these types of errors results in a 1-credit deduction. Any combination of two of these types of errors results in a 2-credit deduction. No more than 2 credits should be deducted for such mechanical errors in any response. The teacher must carefully review the student's work to determine what errors were made and what type of errors they were.

*Conceptual Errors:* A conceptual error involves a more serious lack of knowledge or procedure. Examples of conceptual errors include using the incorrect formula for the area of a figure, choosing the incorrect trigonometric function, or multiplying the exponents instead of adding them when multiplying terms with exponents. A response with one conceptual error can receive no more than half credit.

If a response shows repeated occurrences of the same conceptual error, the student should not be penalized twice. If the same conceptual error is repeated in responses to other questions, credit should be deducted in each response.

If a response shows two (or more) different major conceptual errors, it should be considered completely incorrect and receive no credit.

If a response shows one conceptual error and one computational, graphing, or rounding error, the teacher must award credit that takes into account both errors; i.e., awarding half credit for the conceptual error and deducting 1 credit for each mechanical error (maximum of two deductions for mechanical errors).

**Part II**

For each question, use the specific criteria to award a maximum of two credits. Unless otherwise specified, mathematically correct alternative solutions should be awarded appropriate credit.

- (31)    [2] “No,” and an appropriate justification is given.
- [1] The equations and expressions are correctly categorized, but no justification is given.  
*or*  
[1] An appropriate justification is given, but the question is answered incorrectly.  
[0] “No,” but the justification is missing or incorrect.  
*or*  
[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
- (32)    [2] 5,112, and appropriate work is shown.
- [1] Appropriate work is shown, but one computational error is made.  
*or*  
[1] Appropriate work is shown, but one conceptual error is made, such as not finding the difference.  
*or*  
[1]  $(12)(30)(16) - (6)(9)(12)$  or an equivalent expression, but no further correct work is shown.  
*or*  
[1] 5,112, but no work is shown.  
[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

INTEGRATED ALGEBRA – *continued*

- (33) [2]  $\frac{3}{8}$  or an equivalent answer, and appropriate work is shown.

[1] Appropriate work is shown, but one computational error is made.

*or*

[1] Appropriate work is shown, but one conceptual error is made.

*or*

[1] A correct tree diagram or sample space is shown, but no probability or an incorrect probability is written.

*or*

[1]  $\frac{3}{8}$  or an equivalent answer, but no work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

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**Part III**

For each question, use the specific criteria to award a maximum of three credits. Unless otherwise specified, mathematically correct alternative solutions should be awarded appropriate credit.

- (34) [3]  $x = -2$  and  $(-2, 11)$ , and appropriate algebraic work is shown.

[2] Appropriate work is shown, but one computational error is made.

*or*

[2] An incorrect equation of the axis of symmetry is found, but an appropriate vertex is found.

*or*

[2]  $x = -2$  and  $y = 11$ , and appropriate work is shown, but the vertex is not stated as a point.

[1] Appropriate work is shown, but two or more computational errors are made.

*or*

[1] Appropriate work is shown, but one conceptual error is made, such as not expressing the axis of symmetry as an equation.

*or*

[1]  $x = -2$  and  $(-2, 11)$ , but a method other than algebraic is used.

*or*

[1] Appropriate work is shown to find  $x = -2$ , but no further correct work is shown.

*or*

[1] Appropriate work is shown to find  $(-2, 11)$ , but no further correct work is shown.

*or*

[1]  $x = -2$  and  $(-2, 11)$ , but no work is shown.

[0]  $x = -2$  or  $(-2, 11)$ , but no work is shown.

*or*

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

INTEGRATED ALGEBRA – *continued*

- (35) [3] 30.4, and appropriate work is shown, and “no,” and an appropriate justification is given.
- [2] Appropriate work is shown, but one computational or rounding error is made, but an appropriate answer and justification are given.
- or*
- [2] 30.4, and appropriate work is shown, and “no,” but no justification or an incorrect justification is given.
- [1] Appropriate work is shown, but two or more computational or rounding errors are made, but an appropriate answer and justification are given.
- or*
- [1] Appropriate work is shown, but one conceptual error is made, but an appropriate answer and justification are given.
- or*
- [1] 30.4 and “no,” but no work is shown, and no justification or an incorrect justification is given.
- [0] “No,” but no work is shown, and no justification or an incorrect justification is given.
- or*
- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

INTEGRATED ALGEBRA – *continued*

- (36) [3] Greg, and appropriate work is shown to justify the answer.
- [2] Appropriate work is shown, but one computational error is made, but an appropriate name is stated.
- or*
- [2] Appropriate work is shown computing both rates, but Greg is not stated to have the faster rate.
- [1] Appropriate work is shown, but two or more computational errors are made, but an appropriate name is stated.
- or*
- [1] Appropriate work is shown, but one conceptual error is made, but an appropriate name is stated.
- or*
- [1] Appropriate work is shown to determine one of the rates, but no further correct work is shown.
- [0] Greg, but no work is shown.
- or*
- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.
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**Part IV**

For each question, use the specific criteria to award a maximum of four credits. Unless otherwise specified, mathematically correct alternative solutions should be awarded appropriate credit.

(37)      [4]  $\frac{x-7}{3x}$ , and appropriate work is shown.

- [3] Appropriate work is shown, but one computational, factoring, or simplification error is made.
- [2] Appropriate work is shown, but two or more computational, factoring, or simplification errors are made.

*or*

- [2] Appropriate work is shown, but one conceptual error is made, such as not multiplying by the reciprocal.

*or*

- [2] All numerators and denominators are factored correctly, but no further correct work is shown.
- [1] Appropriate work is shown, but one conceptual error and one computational, factoring, or simplification error are made.

*or*

[1]  $\frac{x-7}{3x}$ , but no work is shown.

- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

INTEGRATED ALGEBRA – *continued*

- (38) [4] Both equations are graphed correctly, and at least one is labeled, and  $(1, -3)$  is stated.

- [3] Appropriate work is shown, but one computational, graphing, or labeling error is made, but an appropriate point of intersection is stated.

*or*

- [3] Both equations are graphed correctly and at least one is labeled, but the point of intersection is not stated or is stated incorrectly.

- [2] Appropriate work is shown, but two or more computational, graphing, or labeling errors are made, but an appropriate point of intersection is stated.

*or*

- [2] Appropriate work is shown, but one conceptual error is made, but an appropriate point of intersection is stated.

*or*

- [2] Both equations are graphed correctly, but neither is labeled, and the point of intersection is not stated or is stated incorrectly.

*or*

- [2]  $(1, -3)$ , but a method other than graphic is used.

- [1] Appropriate work is shown, but one conceptual error and one computational, graphing, or labeling error are made, but an appropriate point of intersection is stated.

*or*

- [1] One line is graphed and labeled correctly, but no further correct work is shown.

*or*

- [1]  $(1, -3)$ , but no work is shown.

- [0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

INTEGRATED ALGEBRA – *continued*

- (39) [4] A box-and-whisker plot is constructed correctly, where the minimum = 66, the first quartile = 72.5, the median = 85, the third quartile = 90, and the maximum = 95.

[3] A box-and-whisker plot is constructed, but one computational or graphing error is made.

[2] A box-and-whisker plot is constructed, but two or more computational or graphing errors are made.

*or*

[2] A box-and-whisker plot is constructed, but one conceptual error is made.

[1] A box-and-whisker plot is constructed, but one conceptual error and one computational or graphing error are made.

*or*

[1] A box-and-whisker plot is constructed, but only two of the statistical measures, the first quartile, the median, or the third quartile are found.

*or*

[1] Minimum = 66, first quartile = 72.5, median = 85, third quartile = 90, and maximum = 95 are found, but no further correct work is shown.

[0] A zero response is completely incorrect, irrelevant, or incoherent or is a correct response that was obtained by an obviously incorrect procedure.

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## Map to Learning Standards

Key Ideas	Item Numbers
Number Sense and Operations	22, 23, 35
Algebra	1, 2, 3, 4, 6, 9, 11, 12, 13, 14, 15, 17, 18, 20, 21, 27, 28, 29, 31, 34, 37
Geometry	16, 19, 24, 25, 32, 38
Measurement	26, 36
Statistics and Probability	5, 7, 8, 10, 30, 33, 39

## Regents Examination in Integrated Algebra August 2009

### Chart for Converting Total Test Raw Scores to Final Examination Scores (Scaled Scores)

The *Chart for Determining the Final Examination Score for the August 2009 Regents Examination in Integrated Algebra* will be posted on the Department's web site <http://www.emsc.nysed.gov/osa/> on Thursday, August 13, 2009. Conversion charts provided for previous administrations of the Integrated Algebra examination must NOT be used to determine students' final scores for this administration.

### Submitting Teacher Evaluations of the Test to the Department

Suggestions and feedback from teachers provide an important contribution to the test development process. The Department provides an online evaluation form for State assessments. It contains spaces for teachers to respond to several specific questions and to make suggestions. Instructions for completing the evaluation form are as follows:

1. Go to [www.emsc.nysed.gov/osa/exameval](http://www.emsc.nysed.gov/osa/exameval).
2. Select the test title.
3. Complete the required demographic fields.
4. Complete each evaluation question and provide comments in the space provided.
5. Click the SUBMIT button at the bottom of the page to submit the completed form.