MATHEMATICS A

The University of the State of New York

REGENTS HIGH SCHOOL EXAMINATION

MATHEMATICS A

Wednesday, August 13, 2008 — 8:30 to 11:30 a.m., only

Print Your Name: 

Print Your School’s Name: 

Print your name and the name of your school in the boxes above. Then turn to
the last page of this booklet, which is the answer sheet for Part I. Fold the last page
along the perforations and, slowly and carefully, tear off the answer sheet. Then fill
in the heading of your answer sheet.

Scrap paper is not permitted for any part of this examination, but you may use
the blank spaces in this booklet as scrap paper. A perforated sheet of scrap graph
paper is provided at the end of this booklet for any question for which graphing may
be helpful but is not required. You may remove this sheet from this booklet. Any work
done on this sheet of scrap graph paper will not be scored. All work should be
written in pen, except graphs and drawings, which should be done in pencil.

This examination has four parts, with a total of 39 questions. You must answer
all questions in this examination. Write your answers to the Part I multiple-choice
questions on the separate answer sheet. Write your answers to the questions in
Parts II, III, and IV directly in this booklet. Clearly indicate the necessary steps,
including appropriate formula substitutions, diagrams, graphs, charts, etc.

When you have completed the examination, you must sign the statement printed
at the end of the answer sheet, indicating that you had no unlawful knowledge of the
questions or answers prior to the examination and that you have neither given nor
received assistance in answering any of the questions during the examination. Your
answer sheet cannot be accepted if you fail to sign this declaration.

Notice. . .
A minimum of a scientific calculator, a straightedge (ruler), and a compass must be available
for you to use while taking this examination.

The use of any communications device is strictly prohibited when taking this
examination. If you use any communications device, no matter how briefly, your
examination will be invalidated and no score will be calculated for you.

DO NOT OPEN THIS EXAMINATION BOOKLET UNTIL THE SIGNAL IS GIVEN.
Part I

Answer all questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. For each question, write on the separate answer sheet the numeral preceding the word or expression that best completes the statement or answers the question. [60]

1. If $6.54 \times 10^n = 65,400$, what is the value of $n$?
   (1) 5  (3) −3
   (2) −5  (4) 4

2. Which letter has both line and point symmetry?
   (1) B  (3) S
   (2) T  (4) H

3. Marilyn selects a piece of candy at random from a jar that contains four peppermint, five cherry, three butterscotch, and two lemon candies. What is the probability that the candy she selects is not a cherry candy?
   (1) 0  (3) $\frac{9}{14}$
   (2) $\frac{5}{14}$  (4) $\frac{14}{14}$

4. The formula for converting temperatures in degrees Celsius to degrees Fahrenheit is $F = \frac{9}{5}C + 32$. If the temperature is 20°C, what is the temperature in degrees Fahrenheit?
   (1) 68  (3) 33.8
   (2) 43.1  (4) 4
5. Andy drives 80 miles to get to the Thruway, drives 100 miles on the Thruway, and then drives an additional 75 miles after leaving the Thruway. If the entire trip took 5 hours and he made no stops, what was his average speed, in miles per hour?

(1) 51  (3) 250
(2) 65  (4) 255

6. Which property is illustrated by the equation $4x(2x - 1) = 8x^2 - 4x$?

(1) associative  (3) distributive
(2) commutative  (4) identity

7. What is the sum of $2m^2 + 3m - 4$ and $m^2 - 3m - 2$?

(1) $m^2 - 6$
(2) $3m^2 - 6$
(3) $3m^2 + 6m - 6$
(4) $m^2 + 6m - 2$

8. In the accompanying diagram, line $n$ is parallel to line $m$, line $t$ is a transversal, and $m\angle 1 = 24$.

What does $x$ equal, in degrees?

(1) 24  (3) 114
(2) 66  (4) 156

Use this space for computations.
9 If a machine that prints designs on T-shirts prints 500 shirts in 3 hours, how many hours will it take to print designs on 1,800 shirts?

(1) 6 (3) 10.8
(2) 9.8 (4) 12

10 The sum of two negative numbers always has to be

(1) negative (3) zero
(2) positive (4) an integer

11 The width, \( w \), of a rectangular rug is 4 less than its length, \( \ell \). Which expression represents the area of the rug?

(1) \( \ell(4 - \ell) \) (3) \( 2(\ell - 4) + 2\ell \)
(2) \( \ell(\ell - 4) \) (4) \( 2w + 2\ell \)

12 What is the value of \( m \) in the equation \( 2m - (m + 1) = 0? \)

(1) 1 (3) \( \frac{1}{3} \)
(2) \(-1\) (4) 0

13 What is the converse of the statement “If \( a^2 + b^2 = c^2 \), then \( \Delta ABC \) is a right triangle”?

(1) If \( \Delta ABC \) is a right triangle, then \( a^2 + b^2 = c^2 \).
(2) \( a^2 + b^2 = c^2 \) if, and only if, \( \Delta ABC \) is a right triangle.
(3) If \( \Delta ABC \) is not a right triangle, then \( a^2 + b^2 \neq c^2 \).
(4) If \( a^2 + b^2 \neq c^2 \), then \( \Delta ABC \) is not a right triangle.
14 Pentagon $ABCDE$ is similar to pentagon $FGHIJ$. The lengths of the sides of $ABCDE$ are 8, 9, 10, 11, and 12. If the length of the longest side of pentagon $FGHIJ$ is 18, what is the perimeter of pentagon $FGHIJ$?

(1) 50  (3) 75  
(2) 56  (4) 100

15 Which inequality is shown on the accompanying graph?

(1) $x < -1$  (3) $x > -1$  
(2) $x \leq -1$  (4) $x \geq -1$

16 A teacher wants to divide her class into groups. Which expression represents the number of different 3-person groups that can be formed from a class of 22 students?

(1) $3!$  (3) $\binom{22}{3}$  
(2) $\binom{22}{3}$  (4) $22 \cdot 21 \cdot 20$

17 What is $6x^3 + 4x^2 + 2x$ divided by $2x$?

(1) $3x^2 + 2x$  
(2) $3x^2 + 2x + 1$  
(3) $4x^2 + 2x$  
(4) $4x^2 + 2x + 1$

18 The greatest common factor of $4a^2b$ and $6ab^3$ is

(1) $2ab$  (3) $12ab$  
(2) $2ab^2$  (4) $24a^3b^4$
19 The statement “Maya plays on the basketball team or Maya joins the ski club” is false. Which statement is true?

(1) Maya plays on the basketball team and Maya joins the ski club.
(2) Maya plays on the basketball team and Maya does not join the ski club.
(3) Maya does not play on the basketball team and Maya joins the ski club.
(4) Maya does not play on the basketball team and Maya does not join the ski club.

20 The measures of five of the interior angles of a hexagon are 150°, 100°, 80°, 165°, and 150°. What is the measure of the sixth interior angle?

(1) 75°  (3) 105°
(2) 80°  (4) 180°

21 For which value of \(x\) is the expression \(\frac{3x - 3}{x - 5}\) undefined?

(1) 1  (3) 5
(2) -1  (4) -5

22 Which point is in the solution set of the system of inequalities shown on the accompanying graph?

(1) (0,0)  (3) (5,2)
(2) (3,3)  (4) (2,3)
23 In the accompanying diagram, the center of circle \( O \) is \((0,0)\), and the coordinates of point \( P \) are \((3,4)\). If \( OP \) is a radius, what is the equation of the circle?

\[
\begin{align*}
(1) & \quad x^2 + y^2 = 5 \\
(2) & \quad x^2 + y^2 = 9 \\
(3) & \quad x^2 + y^2 = 16 \\
(4) & \quad x^2 + y^2 = 25
\end{align*}
\]

24 The expression \((-4a^3b)^2\) is equivalent to

\[
\begin{align*}
(1) & \quad -16a^6b^2 \\
(2) & \quad 16a^6b^2 \\
(3) & \quad 16a^5b^2 \\
(4) & \quad 8a^6b^2
\end{align*}
\]

25 For which equation is the solution set \([-5,2]\)?

\[
\begin{align*}
(1) & \quad x^2 + 3x - 10 = 0 \\
(2) & \quad x^2 - 3x = 10 \\
(3) & \quad x^2 + 3x = -10 \\
(4) & \quad x^2 - 3x + 10 = 0
\end{align*}
\]

26 When the Smith family decided to have their new house built, they found that there were 60 different choices involving location, style, and color. If they had their choice of 2 locations and 5 styles, how many choices of color did they have?

\[
\begin{align*}
(1) & \quad 6 \\
(2) & \quad 12 \\
(3) & \quad 50 \\
(4) & \quad 53
\end{align*}
\]
27 In a survey, 450 high school students were asked for their preference of fast food for lunch. The accompanying circle graph represents the results.

![Circle Graph]

How many students preferred salad?
(1) 60  (3) 150
(2) 75  (4) 300

28 A line with a slope of $\frac{1}{3}$ passes through the point (3,6). Which point also lies on this line?
(1) (6,3)  (3) (−3,−3)
(2) (7,6)  (4) (−6,3)
29 Which statement is logically equivalent to “If I sleep, then I will not eat”?

(1) If I do not sleep, then I will eat.
(2) If I eat, then I will not sleep.
(3) If I eat, then I will sleep.
(4) If I do not eat, then I will sleep.

30 Phil is cutting a triangular piece of tile. If the triangle is scalene, which set of numbers could represent the lengths of the sides?

(1) {2, 4, 7}    (2) {4, 5, 6}    (3) {3, 5, 8}    (4) {5, 5, 8}
Part II

Answer all questions in this part. Each correct answer will receive 2 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. [10]

31 Solve for $x$: $0.35x + 0.6 = 0.1x + 1$
32 The accompanying diagram shows intersecting lines \( \ell \) and \( m \). Solve for the value of \( x \).
33 Theo determined that the correct length of the hypotenuse of the right triangle in the accompanying diagram is $\sqrt{20}$. Fiona found the length of the hypotenuse to be $2\sqrt{5}$. Is Fiona’s answer also correct? Justify your answer.
34 One endpoint of a line segment is (6,2). The midpoint of the segment is (2,0). Find the coordinates of the other endpoint. [The use of the accompanying grid is optional.]
35 Using a compass and straightedge, construct the line that is perpendicular to $\overline{AB}$ and that passes through point $P$. Show all construction marks.
36 The mean of three numbers is 25. The second number is four less than twice the first. The third number is two more than four times the first. Find the smallest number.
A billboard on level ground is supported by a brace, as shown in the accompanying diagram. The measure of angle $A$ is $15^\circ$ greater than twice the measure of angle $B$. Determine the measure of angle $A$ and the measure of angle $B$. 
On the accompanying set of axes, draw ΔABC, whose coordinates are A(−7,9), B(−2,8), and C(−3,4). Then draw, label, and state the coordinates of ΔA′B′C′, the image of ΔABC after the transformation that maps (x,y) to (−x,−y). Based on your diagram, identify the type of transformation that was performed.
39 Solve the following system of equations algebraically or graphically for $x$ and $y$:

\[
\begin{align*}
y &= x^2 + 4x + 6 \\
y &= 2x + 6
\end{align*}
\]
Scrap Graph Paper — This sheet will not be scored.
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ANSWER SHEET

Student

Sex: □ Male □ Female

Teacher

School

Your answers to Part I should be recorded on this answer sheet.

Part I

Answer all 30 questions in this part.

1 9 17 25
2 10 18 26
3 11 19 27
4 12 20 28
5 13 21 29
6 14 22 30
7 15 23
8 16 24

Your answers for Parts II, III, and IV should be written in the test booklet.

The declaration below should be signed when you have completed the examination.

I do hereby affirm, at the close of this examination, that I had no unlawful knowledge of the questions or answers prior to the examination and that I have neither given nor received assistance in answering any of the questions during the examination.

Signature
### MATHEMATICS A

<table>
<thead>
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Rater’s/Scorer’s Name (minimum of three)

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