# Thursday，August 17， 2023 －12：30 to 3：30 p．m．，only 

## Student Name：

## School Name：

$\qquad$
The possession or use of any communications device is strictly prohibited when taking this examination．If you have or use any communications device，no matter how briefly，your examination will be invalidated and no score will be calculated for you．

Print your name and the name of your school on the lines above．
A separate answer sheet for Part I has been provided to you．Follow the instructions from the proctor for completing the student information on your answer sheet．

This examination has four parts，with a total of 35 questions．You must answer all questions in this examination．Record your answers to the Part I multiple－choice questions on the separate answer sheet．Write your answers to the questions in Parts II，III，and IV directly in this booklet． All work should be written in pen，except graphs and drawings，which should be done in pencil．Clearly indicate the necessary steps，including appropriate formula substitutions，diagrams， graphs，charts，etc．Utilize the information provided for each question to determine your answer． Note that diagrams are not necessarily drawn to scale．

The formulas that you may need to answer some questions in this examination are found at the end of the examination．This sheet is perforated so you may remove it from this booklet．

Scrap paper is not permitted for any part of this examination，but you may use the blank spaces in this booklet as scrap paper．A perforated sheet of scrap graph paper is provided at the end of this booklet for any question for which graphing may be helpful but is not required．You may remove this sheet from this booklet．Any work done on this sheet of scrap graph paper will not be scored．

When you have completed the examination，you must sign the statement printed at the end of the answer sheet，indicating that you had no unlawful knowledge of the questions or answers prior to the examination and that you have neither given nor received assistance in answering any of the questions during the examination．Your answer sheet cannot be accepted if you fail to sign this declaration．

[^0]
## DO NOT OPEN THIS EXAMINATION BOOKLET UNTIL THE SIGNAL IS GIVEN．

## Part I

Answer all 24 questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For each statement or question, choose the word or expression that, of those given, best completes the statement or answers the question. Record your answers on your separate answer sheet. [48]

1 A plane intersects a sphere. Which two-dimensional shape is formed by this cross section?
(1) rectangle
(3) square
(2) triangle
(4) circle

2 The endpoints of $\overline{A B}$ are $A(-5,3)$ and $B(7,-5)$. Point $P$ is on $\overline{A B}$ such that $A P: P B=3: 1$. What are the coordinates of point $P$ ?
(1) $(-2,-3)$
(3) $(-2,1)$
(2) $(1,-1)$
(4) $(4,-3)$

## Use this space for computations.

4 Darnell models a cup with the cylinder below. He measured the

## Use this space for computations.

 diameter of the cup to be 10 cm and the height to be 9 cm .

If Darnell fills the cup with water to a height of 8 cm , what is the volume of the water in the cup, to the nearest cubic centimeter?
(1) 628
(3) 2513
(2) 707
(4) 2827

5 Which quadrilateral has diagonals that are always perpendicular?
(1) rectangle
(3) trapezoid
(2) rhombus
(4) parallelogram

6 Which regular polygon would carry onto itself after a rotation of $300^{\circ}$ about its center?
(1) decagon
(3) octagon
(2) nonagon
(4) hexagon

7 The rectangle drawn below is continuously rotated about side $S$.

Use this space for computations.


Which three-dimensional figure is formed by this rotation?
(1) rectangular prism
(3) cylinder
(2) square pyramid
(4) cone

8 An equation of the line perpendicular to the line whose equation is $4 x-5 y=6$ and passes through the point $(-2,3)$ is
(1) $y+3=-\frac{5}{4}(x-2)$
(3) $y+3=\frac{4}{5}(x-2)$
(2) $y-3=-\frac{5}{4}(x+2)$
(4) $y-3=\frac{4}{5}(x+2)$

9 In circle $P$ below, diameter $\overline{A C}$ and radius $\overline{B P}$ are drawn such that $\mathrm{m} \angle A P B=110^{\circ}$.


If $A C=12$, what is the area of shaded sector $B P C$ ?
(1) $\frac{7}{6} \pi$
(3) $11 \pi$
(2) $7 \pi$
(4) $28 \pi$

## Use this space for computations.

10 In $\triangle A B C$, side $\overline{B C}$ is extended through $C$ to $D$. If $\mathrm{m} \angle A=30^{\circ}$ and $\mathrm{m} \angle A C D=110^{\circ}$, what is the longest side of $\triangle A B C$ ?
(1) $\overline{A C}$
(3) $\overline{A B}$
(2) $\overline{B C}$
(4) $\overline{C D}$

11 Right triangle $A C T$ has $\mathrm{m} \angle A=90^{\circ}$. Which expression is always equivalent to cos $T$ ?
(1) $\cos C$
(3) $\tan T$
(2) $\sin C$
(4) $\sin T$

12 A regular pyramid with a square base is made of solid glass. It has a base area of $36 \mathrm{~cm}^{2}$ and a height of 10 cm . If the density of glass is 2.7 grams per cubic centimeter, the mass of the pyramid, in grams, is
(1) 120
(3) 360
(2) 324
(4) 972

13 The equation of a circle is $x^{2}+y^{2}+12 x=-27$. What are the coordinates of the center and the length of the radius of the circle?
(1) center $(6,0)$ and radius 3
(2) center $(6,0)$ and radius 9
(3) center $(-6,0)$ and radius 3
(4) center $(-6,0)$ and radius 9

14 In triangle $A B C$ below, $D$ is a point on $\overline{A B}$ and $E$ is a point on $\overline{A C}$,

Use this space for computations. such that $\overline{D E} \| \overline{B C}$.


If $A D=12, D B=8$, and $E C=10$, what is the length of $\overline{A C}$ ?
(1) 15
(3) 24
(2) 22
(4) 25

15 In the diagram below, point $E$ is located inside square $A B C D$ such that $\triangle A B E$ is equilateral, and $\overline{C E}$ is drawn.


What is $\mathrm{m} \angle B E C$ ?
(1) $30^{\circ}$
(3) $75^{\circ}$
(2) $60^{\circ}$
(4) $90^{\circ}$

16 In the diagram below of quadrilateral $A D B E, \overline{D E}$ is the perpendicular

## Use this space for computations.

 bisector of $\overline{A B}$.

Which statement is always true?
(1) $\angle A D C \cong \angle B D C$
(3) $\overline{A D} \cong \overline{B E}$
(2) $\angle E A C \cong \angle D A C$
(4) $\overline{A E} \cong \overline{A D}$

17 What is the image of $(4,3)$ after a reflection over the line $y=1$ ?
(1) $(-2,3)$
(3) $(4,-1)$
(2) $(-4,3)$
(4) $(4,-3)$

18 In the diagram below, a cone has a diameter of 16 inches and a slant height of 17 inches.


What is the volume of the cone, in cubic inches?
(1) $320 \pi$
(3) $960 \pi$
(2) $363 \pi$
(4) $1280 \pi$

19 In the diagram below, lines $\ell$ and $m$ intersect lines $n$ and $p$ to create

Use this space for computations. the shaded quadrilateral as shown.


Which congruence statement would be sufficient to prove the quadrilateral is a parallelogram?
(1) $\angle 1 \cong \angle 6$ and $\angle 9 \cong \angle 14$
(2) $\angle 5 \cong \angle 10$ and $\angle 6 \cong \angle 9$
(3) $\angle 5 \cong \angle 7$ and $\angle 10 \cong \angle 15$
(4) $\angle 6 \cong \angle 9$ and $\angle 9 \cong \angle 11$

20 In the circle below, secants $\overline{T S R}$ and $\overline{T M H}$ intersect at $T, S R=5$, $H M=9, T M=3$, and $T S=x$.


Which equation could be used to find the value of $x$ ?
(1) $x(x+5)=36$
(3) $3 x=45$
(2) $x(x+5)=27$
(4) $5 x=27$

21 On the set of axes below, the coordinates of three vertices of trapezoid $A B C D$ are $A(2,1), B(5,4)$, and $D(-2,3)$.


Which point could be vertex $C$ ?
(1) $(1,5)$
(3) $(-1,6)$
(2) $(4,10)$
(4) $(-3,8)$

22 In the diagram below, $\triangle A B C \cong \triangle D E C$.

## Use this space for computations.



Which transformation will map $\triangle A B C$ onto $\triangle D E C$ ?
(1) a rotation
(2) a line reflection
(3) a translation followed by a dilation
(4) a line reflection followed by a second line reflection

23 If $\triangle T A P$ is dilated by a scale factor of 0.5 , which statement about the image, $\triangle T^{\prime} A^{\prime} P^{\prime}$, is true?
(1) $\mathrm{m} \angle T^{\prime} A^{\prime} P^{\prime}=\frac{1}{2}(\mathrm{~m} \angle T A P)$
(2) $\mathrm{m} \angle T^{\prime} A^{\prime} P^{\prime}=2(\mathrm{~m} \angle T A P)$
(3) $T A=2\left(T^{\prime} A^{\prime}\right)$
(4) $T A=\frac{1}{2}\left(T^{\prime} A^{\prime}\right)$

Use this space for computations.

24 In the diagram below of $\triangle A B C, X$ and $Y$ are points on $\overline{A B}$ and $\overline{A C}$, respectively, such that $\mathrm{m} \angle A Y X=\mathrm{m} \angle B$.


Which statement is not always true?
(1) $\frac{A X}{A C}=\frac{X Y}{C B}$
(3) $(A Y)(C B)=(X Y)(A B)$
(2) $\frac{A Y}{A B}=\frac{A X}{A C}$
(4) $(A Y)(A B)=(A C)(A X)$

## Part II

Answer all 7 questions in this part. Each correct answer will receive 2 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [14]

25 On the set of axes below, congruent quadrilaterals $R O C K$ and $R^{\prime} O^{\prime} C^{\prime} K^{\prime}$ are graphed.


Describe a sequence of transformations that would map quadrilateral $R O C K$ onto quadrilateral $R^{\prime} O^{\prime} C^{\prime} K^{\prime}$.

26 In triangle $C E M, C E=3 x+10, M E=5 x-14$, and $C M=2 x-6$.
Determine and state the value of $x$ that would make $\triangle C E M$ an isosceles triangle with the vertex angle at $E$.

27 A flagpole casts a shadow on the ground 91 feet long, with a $53^{\circ}$ angle of elevation from the end of the shadow to the top of the flagpole.

Determine and state, to the nearest tenth of a foot, the height of the flagpole.

28 A man is spray-painting the tops of 10 patio tables. Five tables have round tops, with diameters of 4 feet, and five tables have rectangular tops, with dimensions of 4 feet by 6 feet. A can of spray paint covers 25 square feet. How many cans of spray paint must be purchased to paint all of the tabletops?

29 Using a compass and straightedge, construct a midsegment of $\triangle A H L$ below. [Leave all construction marks.]


30 Right triangle $S T R$ is shown below, with $\mathrm{m} \angle T=90^{\circ}$. Altitude $\overline{T Q}$ is drawn to $\overline{S Q R}$, and $T Q=8$.


If the ratio $S Q: Q R$ is $1: 4$, determine and state the length of $\overline{S R}$.

31 Line $A B$ is dilated by a scale factor of 2 centered at point $A$.


Evan thinks that the dilation of $\overleftrightarrow{A B}$ will result in a line parallel to $\overleftrightarrow{A B}$, not passing through points $A$ or $B$.

Nathan thinks that the dilation of $\overleftrightarrow{A B}$ will result in the same line, $\overleftrightarrow{A B}$.
Who is correct?
Explain why.

## Part III

Answer all 3 questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [12]

32 Josh is making a square-based fire pit out of concrete for his backyard, as modeled by the right prism below. He plans to make the outside walls of the fire pit 3.5 feet on each side with a height of 1.5 feet. The concrete walls of the fire pit are going to be 9 inches thick.


If a bag of concrete mix will fill $0.6 \mathrm{ft}^{3}$, determine and state the minimum number of bags needed to build the fire pit.

33 A telephone pole 11 meters tall needs to be stabilized with a support beam, as modeled below.


Two conditions for proper support are:

- The beam reaches the telephone pole at $70 \%$ of the telephone pole's height above the ground.
- The beam forms a $65^{\circ}$ angle with the ground.

Determine and state, to the nearest tenth of a meter, the length of the support beam that meets these conditions for this telephone pole.

Determine and state, to the nearest tenth of a meter, how far the support beam must be placed from the base of the pole to meet the conditions.

34 The coordinates of the vertices of quadrilateral $A B C D$ are $A(0,4), B(3,8), C(8,3)$, and $D(5,-1)$. Prove that $A B C D$ is a parallelogram, but not a rectangle.
[The use of the set of axes below is optional.]


## Part IV

Answer the question in this part. A correct answer will receive 6 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided to determine your answer. Note that diagrams are not necessarily drawn to scale. A correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [6]

35 In the diagram below of quadrilateral $F A C T, \overline{B R}$ intersects diagonal $\overline{A T}$ at $E$, $\overline{A F} \| \overline{C T}$, and $\overline{A F} \cong \overline{C T}$.


Prove: $(A B)(T E)=(A E)(T R)$

## Question 35 continued

Scrap Graph Paper - this sheet will not be scored.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  | , |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| - |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| , |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  | - |  |  | - | - |  | - |  |  | - |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  | - |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

Scrap Graph Paper - this sheet will not be scored.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## High School Math Reference Sheet

| 1 inch $=2.54$ centimeters | 1 kilometer $=0.62$ mile | 1 cup $=8$ fluid ounces |
| :--- | :--- | :--- |
| 1 meter $=39.37$ inches | 1 pound $=16$ ounces | 1 pint $=2$ cups |
| 1 mile $=5280$ feet | 1 pound $=0.454$ kilogram | 1 quart $=2$ pints |
| 1 mile $=1760$ yards | 1 kilogram $=2.2$ pounds | 1 gallon $=4$ quarts |
| 1 mile $=1.609$ kilometers | 1 ton $=2000$ pounds | 1 gallon $=3.785$ liters |
|  |  | 1 liter $=0.264$ gallon |
|  | 1 liter $=1000$ cubic centimeters |  |


| Triangle | $A=\frac{1}{2} b h$ |
| :--- | :--- |
| Parallelogram | $A=b h$ |
| Circle | $A=\pi r^{2}$ |
| Circle | $C=\pi d$ or $C=2 \pi r$ |
| General Prisms | $V=B h$ |
| Cylinder | $V=\pi r^{2} h$ |
| Sphere | $V=\frac{4}{3} \pi r^{3}$ |
| Cone | $V=\frac{1}{3} \pi r^{2} h$ |
| Pyramid | $V=\frac{1}{3} B h$ |


| Pythagorean <br> Theorem | $a^{2}+b^{2}=c^{2}$ |
| :--- | :--- |
| Quadratic <br> Formula | $x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$ |
| Arithmetic <br> Sequence | $a_{n}=a_{1}+(n-1) d$ |
| Geometric <br> Sequence | $a_{n}=a_{1} r^{n-1}$ |
| Geometric <br> Series | $S_{n}=\frac{a_{1}-a_{1} r^{n}}{1-r}$ where $r \neq 1$ |
| Radians | 1 radian $=\frac{180}{\pi}$ degrees |
| Degrees | 1 degree $=\frac{\pi}{180}$ radians |
| Exponential <br> Growth/Decay | $A=A_{0} e^{k\left(t-t_{0}\right)}+B_{0}$ |


[^0]:    Notice ．．．
    A graphing calculator，a straightedge（ruler），and a compass must be available for you to use while taking this examination．

